THERMAL MECHANICAL, LOW CYCLE FATIGUE OF 25 CD4 STEEL

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This study was undertaken to develop an understanding of the fatigue resistance of 25 CD4 steel under conditions of combined thermal and mechanical strain cycling in air. Comparative evolutions were made with existing thermal mechanical fatigue data on Cr-Mo steel and with results of a comprehensive, companion study of the fatigue behaviour of this same steel under isothermal conditions. Thermal mechanical fatigue behaviour was investigated for constant amplitude, fully reversed, strain cycling of uniaxially loaded specimens at two ranges of temperature a) 100 to 300° C b) 100 to 500° C and strain in phase with maximum temperature.

### INTRODUCTION

Mechanical equipment and structural components are often subjected to cyclic straining while operating at elevated temperature and thermal fatigue is a recognized failure mode as for structures such as gas turbine components with combined temperature and strain cycling. The only results in phase thermal mechanical cycling were those reported by some authors (1,2,3,4). In some examples the temperature may be constant, while, in other cases, the cyclic straining may be accompanied by thermal cycling. The problem becomes for more complex when the relationship between temperatures and strain must the taken into account. This paper described the results of a study where the low cycle fatigue behaviour of 25 CD4 steel was investigated for conditions of combined thermal and mechanical strain cycling. Experiments were limited to the extreme condition of in phase cycling and a model based on a relationship between thermal fatigue strength and low cycle fatigue strength is proposed and discussed.

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## EXPERIMENTAL PROCEDURE

The thermal mechanical fatigue experiments are conducted using a servocontrolled electrohydraulic machine. The axial mechanical strain and temperature were controlled to follow one of the both strain and temperature were controlled to follow one of the both basic constant amplitude waveforms shown in Fig. 1:  $\varepsilon$  is in phase with T . The control program wavefrom was provided by a function generator. Heating rate was constant and determined by the thermal response of the specimens and the heating equipment with the length of the thermal cycle maintained at about  $2\frac{1}{2}$  min (T = 300° C, T = 100° C) or 5 mn (T = 500° C, T = 300° C). The total strain amplitude  $\Delta \mathcal{E}_{\mathcal{E}}$ varies from 0,1 % to 1,2 %.

The chemical composition of the sheet is shown in table I.

							1	·	
Element	С	S	Р	Si	Mn	Ni	Cr	Мо	V
Weight %	0,26	0,009	0,012	0,325	0,635	0,56	1,08	0,980	0,3

Table I

Experimental conditions in isothermal low cylce fatigue are as follows;

- strain rate  $3.2 \cdot 10^{-3} \text{s}^{-1}$ 

- testing temperature 100° C - 300° C - 500° C

RESULTS : Isothermal low cyle fatigue

Experimental relations between the total strain rage  $_{\Delta\epsilon}$  /2 and the number of cycles to failure N  $_R$  is shown in table II : t

Δε t/2	0,3 %	0,5 %	0,7 %	1 %	1,2 %
500° C 300° C 100° C	3 300	1 116 2 485 3 735	1 120 1 550	330 673 705	500 508

Table II

The total strain amplitude can be separated into its elastic and plastic components. In low cycle fatigue testing, the plastic component of the strain amplitude is characterized by the fatigue ductility properties and the elastic component by the fatigue strength properties of the material according to MANSON COFFIN BASQUIN equations:

$$\frac{\Delta \varepsilon}{2} = \frac{\sigma' f}{E} \cdot (2 N_R)^b$$
 (1)

$$\frac{\Delta \varepsilon_{p}}{2} = {\varepsilon \choose f} \cdot (2N_{R})^{C}$$
 (2)

$$\frac{\Delta \varepsilon_{t}}{2} = \frac{\Delta \varepsilon_{p}}{2} + \frac{\Delta \varepsilon_{e}}{2}$$
 (3)

with b = fatigue strength exponent
 c = fatigue ductility exponent

The different parameters of these equations are shown in table  $\ensuremath{\text{III}}$ 

T°	С	σ <sub>f</sub> /Ε( %)	b	ε'f (%)	С
3	00	0,451	- 0,0737	52,396	- 0,648
	800	0,459	- 0,0758	50,363	- 0,659
	800	0,367	- 0,0849	43,797	- 0,698

Table III

Thermal mechanical, low cycle fatigue

Typical hysteresis loop generated in type 25 CD4 stainless steel in shown in Fig. 2 Results of all experiments are summarized in table IV.

	N <sub>R</sub> (cycles)		
$\frac{\Delta \varepsilon_{t}}{2}$ (%)	ΔT : 100 à 500° C	ΔT : 300 à 500° C	
1,21 1,01 0,7 0,505 0,5 0,1 0,014	183 210 583 2 690 3 000 430 2 500	230 397 1 185 - - 615 936	

Table III

#### DISCUSSION

According to JASKE (2) plastic strain in thermochanical fatigue  $\Delta \varepsilon_{\mbox{ptm}}$  is defined by the relation

$$\Delta \varepsilon_{\text{ptm}} = \Delta \varepsilon_{\text{t}} - (\overline{E}) T_{\text{max}} - (\overline{E}) T_{\text{min}}$$
 (4)

TAIRA /4/ has suggested the use of the concept of an equivalent temperature for correlating thermal fatigue behaviour with isothermal behaviour. This concept states that, regarding thermal fatigue cycling between two temperatures, the same fatigue life will be developed by isothermal cycling at the equivalent temperature.

As for thermal fatigue of 0.16 percent carbon steel it was shown that the equivalent temperature was defined as follows

$$T_{e} = \frac{T_{\text{max}} + T_{\text{min}}}{2} \quad \text{for } T_{\text{max}} < 400^{\circ} \text{ C}$$
 (5)

$$T_e = T_{\text{max}}$$
 for  $T_{\text{max}} > 500^{\circ} \text{ C}$  (6)

The experimental results are shown in Table V and they are compared with the life prediction given by TAIRA'S concept.

$\Delta T = (300^{\circ} \text{ C}) - 500^{\circ} \text{ C}$ $T_{e} = 400$						
<u>Δε</u> %	Δε <sub>ptm</sub>	N <sub>R</sub> cycles	N <sub>R</sub> cycles			
	2					
1,2	0,979	183	322			
1	0,857	210	392			
0,7	0,498	583	873			
0,505	0,304	2 690	1800			
0,5	0,293	3 000	1910			
0,1	0,263	430	2230			
0,014	0,204	2 500	3240			

ΔΤ	Te= 300°C		
<u>∆</u> €t %	Δε ptm %	N <sub>R</sub> cycles	N <sub>R</sub> cycles
1,2 1 0,7 0,1 0,014	0,974 0,783 0,511 0,312 0,237	230 397 1 185 615 936	398 555 1060 2240 3400

Table V

<code>DEGALLAIX</code> / 5 / et al fit the damage with the following expression where Al, Bl, A2, B2 are material constants and Q is an apparent activation energy. The values obtained from a computer code are for our material

$$\frac{1}{N_{R}} = A_{1} (\Delta \varepsilon_{p})^{B} 1 \exp \left(-\frac{Q}{RT}\right) + A_{2} (\Delta \varepsilon_{p})^{B} 2$$
 (7)

A1 = 70 550 10<sup>-5</sup>
B1 = 1,334
A2 = 224 10<sup>-5</sup>
B2 = 1,543
R = 2 10<sup>-3</sup> Kcal/mole.K
Q = 8,891 Kcal/mole K

From eq.(7)it is clear that in an isothermal fatigue tests and during each half cycle, plastic strain  $\delta \varepsilon_p$  changes from the value 0 to  $\Delta \rho_b$  and damage  $\delta \phi$  from 0 to  $\Delta \rho$  as :

$$\delta \varphi = \frac{A_1}{2} \delta \varepsilon_p^{b_1} \exp \left(-\frac{Q}{Rt}\right) + \frac{A_2}{2} \delta \varepsilon_p^{b_2}$$
 (8)

Although eq. (8) describes originally isothermal damage, it is assumed that this equation is applicable to thermal fatigue in which the variation of T has to be considered. Then the increment of damage  $d(\delta\varphi)$ , connected with the increments of plastic strain  $d(\delta\epsilon p)$  and of temperature dT, is given, differentiating eq.(8)by :

$$d(\delta \boldsymbol{\varphi}) = \begin{bmatrix} \frac{A_1 B_1}{2} & B_1^{-1} \\ \frac{B_1}{2} & \frac{B_1}{p} \end{bmatrix} \exp(-\frac{Q}{RT}) + \frac{A_2 B_2}{2} \delta \varepsilon_p^{B_2^{-1}} d(\delta \varepsilon_p) + \begin{bmatrix} \frac{A_1}{2} & \delta \varepsilon_p^{B_1} \\ \frac{A_1}{2} & \delta \varepsilon_p^{B_1} \end{bmatrix} \frac{Q}{RT^2} \exp(-\frac{Q}{RT}) dT$$
(9)

With numerical values  $\boldsymbol{\mathcal{E}}_p$  and T taken on the stabilized hysteresis loop, the integration of eq.(9) allows the damage evaluation during the heating  $(T_1 \rightarrow T_2)$  and cooling  $(T_2 \rightarrow T_1)$  paths.

Then the thermal fatigue damage per cycle, i.e :

gives an estimation of the fatigue life. By using eq(1), parameters  $^{\Delta\epsilon}$  p and T of equivalent isothermal tess can be determined.

Making up evolution of  $\frac{\Delta\varepsilon_p}{2}$  as a function of temperature results are shown in table VI.  $\frac{\Delta\varepsilon_p}{2}$ 

ΔT: 300	° C-500° C	DEGALLAIX	ΔΤ : 100° C-500° C		DEGALLAIX
$\frac{\Delta \varepsilon t}{2}$ %	N <sub>R</sub> (cycles)	N <sub>R</sub> (cycles)	$\frac{\Delta \varepsilon t}{2}$ %	N <sub>R</sub> (cycles)	N <sub>R</sub> (cycles)
1,21 1 0,7 0,505 0,5 0,1 0,014	183 210 583 2 690 3 000 430 2 500	332 439 904 1 900 1 980 2 740 4 320	1,21 1 0,7 0,1 0,014	230 397 1 185 615 936	395 547 1 040 2 490 3 910

Table VI

The fatigue life values obtained from experiments were much lower than life predicted from isothermal fatigue data. Results of the thermal mechanical fatigue experiments are compared with the isothermal fatigue data in terms of  $\Delta \epsilon$  in fig. 3.

Based on  $\Delta \varepsilon_{\rm f}/2$  (also true for  $\Delta \varepsilon_{\rm f}/2/2$ ) the thermal mechanical results fell below the isothermal results. In thermal mechanical fatigue it is necessary to take into account the evolution of thermal strain. So the mechanical strain  $\Delta \varepsilon_{\rm m}$  can be written by the equations

$$\Delta \epsilon_{m} = \Delta \epsilon_{t} - \Delta \epsilon_{th} \text{ for } \Delta \epsilon_{t} > \Delta \epsilon_{th}$$

$$\alpha$$

$$\Delta_{m} = \Delta \epsilon_{t} + \Delta \epsilon_{th} \text{ for } \Delta \epsilon_{t} < \Delta \epsilon_{th}$$
(11)
(12)

where  $\Delta \xi_{th}$  represents thermal strain between T<sub>max</sub> and T<sub>min</sub>. Table VII gives the values of  $\Delta \xi_m/2$  for different experiments.

	<u>δε<sub>t</sub></u> (%)	Δ T(° C)	$\frac{\Delta \varepsilon_{\text{m}}}{2}$ (%)	N <sub>R</sub> cycles
$^{\Delta\varepsilon}$ t> $^{\Delta\varepsilon}$ th + 0,2 % $^{\Delta\varepsilon}$ m = $^{\Delta\varepsilon}$ t - $^{\Delta\varepsilon}$ th	1,21 1,21 1 0,7 0,7 0,505 0,5	300-500 100-500 300-500 100-500 300-500 100-500 300-100 300-500	0,936 0,814 0,731 0,614 0,426 0,312 0,226 0,221	183 230 210 397 583 1 185 2 690 3 000
$^{\Delta\varepsilon}$ t< $^{\Delta\varepsilon}$ th - 0,2 % $^{\Delta\varepsilon}$ m = $^{\Delta\varepsilon}$ t $^{\Delta\varepsilon}$ th	0,1 0,014 0,1 0,014	100-500 100-500 300-500 300-500	0,496 0,406 0,379 0,293	615 936 430 2 500
		$\frac{\Delta \epsilon_{\text{th}}}{2} = 0,396 \% \text{ (}$ $\frac{\Delta \epsilon_{\text{th}}}{2} = 0,279 \% \text{ (}$		

Table VII

Life as a function of mechanical strain in thermal fatigue  $\Delta \mathcal{E}_m,$  plastic strain in isothermal fatigue is shown in Fig. 4 The relation between mechanical strain and life is given by the equation

equation between mechanical strain and life is given between 
$$^{\Delta\varepsilon}$$
 = 12,16 N<sub>R</sub>  $^{-0,505}$  (13)

We can see in fig.5 that straight line breaksthrough the plastic strain lines in isothermal fatigue for three points A,B,C corresponding with the thermal strain amplitude between 20°C and the considered temperature as it is seen in Table VIII.

T(°C)	Poi	$\frac{\Delta \varepsilon}{12}$ th 20-T°C	
	position	value of Δε/2(%)	
100 300 500	A B C	0,07 0,12 0,43	0,06 0,19 0,40

Table VIII

So we can write that thermal mechanical fatigue experiments with mechanical strain ,  $\Delta \epsilon$  m , are equivalent to isothermal fatigue experiments with plastic strain, $\Delta \varepsilon$  p. For each temperature in isothermal fatigue, the number of cycles to failure,  $N_{R}$ , can be expressed as

$$N_{R} = \left(\frac{\Delta \varepsilon_{\mathbf{p}}}{2 \varepsilon^{\mathbf{r}} \mathbf{f} T}\right)^{1/C} T = g \left(\frac{\Delta \varepsilon_{\mathbf{m}}}{2}\right)^{S}$$
 (14)

Where  $\mathrm{C}_{\mathsf{T}}$  and  $\mathrm{C}_{\mathsf{f}\mathsf{T}}$  are the coefficients of the MANSON COFFIN law at the considered temperature, T, in isothermal experiments, g and s are material constants no functions of temperature. Mechanical strain can be written  $\Delta \epsilon = \lambda (T_1 + 20^\circ \text{ C})$  but neglecting thermal strain between 0 and 20 °C we obtain  $\Delta \epsilon_{\text{m}} = \lambda T_{\text{i}}$  so equation 14

$$g(\frac{\sqrt[4]{Ti}}{2})^{S} = (\frac{\sqrt[4]{Ti}}{2\mathcal{E}^{\dagger}f_{T}})^{T/CT}$$
(15)

can be written: 
$$g(\frac{\sqrt[]{Ti}}{2})^{S} = (\frac{\sqrt[]{Zi}}{2E^{T}f_{T}})^{S}$$
 (15) and  $N_{R} = g(\frac{\Delta \epsilon_{m}}{2})^{S}$  (16)

Material constants g and s, are determined from the MANSON COFFIN coefficients in isothermal experiments, which give an  $\ensuremath{\mathsf{N}}$ estimation of the thermoméchanical fatigue life using equation.16.

For the 25 CD4, the value of constants g and s in equation (16) are obtained from the test results as follows:  $g = 11,68 \cdot 10^{-3}$ 

$$g = 11,68 10$$
  
 $s = -2,022$ 

Also shown in Fig. 6 calculated fatigue lifes using isothermal fatigue curves are compared with experimental thermal-mechanical fatigue life.  $\Delta \epsilon_{m}$  On the basis of 2 versus  $N_{D}$ , the thermal-mechanical fatigue On the basis of  $\frac{1}{2}$  versus  $N_{R}$ , the thermal-mechanical fatigue life is well correlated with the sothermal fatigue life.

### CONCLUSION

Many criteria for thermal fatigue failure have been proposed but almost all of them seem to be little authorized. Both of the combined effects of temperature and strain as well as the wide variations of test methods make it difficult to find a general

The experimental results in thermal-mechanical fatigue were compared with the predicted life of the material obtained from the low cycle fatigue data at constant temperatures. The results obtained are summarized as follows :

The relationship between the mechanical strain range  $\Delta \epsilon$  and the number of cycles to failure N<sub>D</sub> under fixed Tmax and TmTn can be described by  $\Delta \epsilon$  = 12,16NR-0,505 A model based on a relationship between thermal fatigue and low

cycle fatigue strength is proposed. According to the relation

$$g\left(\frac{AT}{2}\right)^{S} = \left(\frac{AT}{2\epsilon' f_{T}}\right)^{1/C}T = N_{R}$$

we observe good agreement between experimental results and those predicted by the proposed model.

#### REFERENCES

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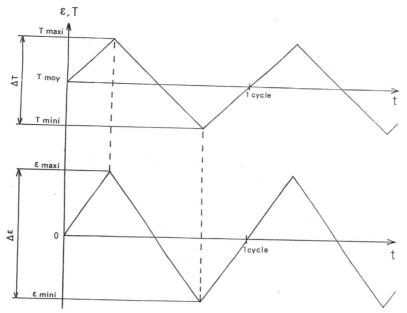


Figure 1 : Illustration of control waveforms

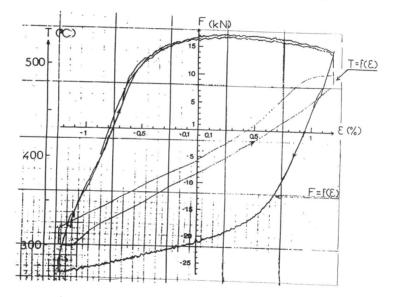
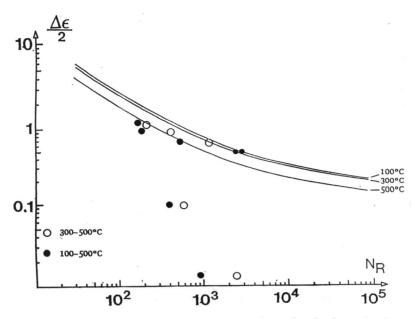
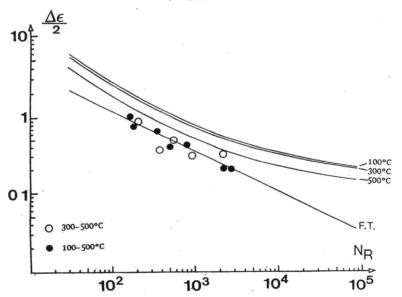


Figure 2 : Stress-strain hysteresis loop for 300 to 500° C cycle with  $\epsilon_{\rm max}$  at Tmax



 $\frac{\text{Figure 3}}{\text{on 25CD4 steel}}: \text{ Isothermal and thermal cycle fatigue tests}$ 



 $\frac{\text{Figure 4}}{\text{ with total strain in low cycle fatigue}} \; : \; \text{Comparison of mechanical strain in thermal fatigue}$ 

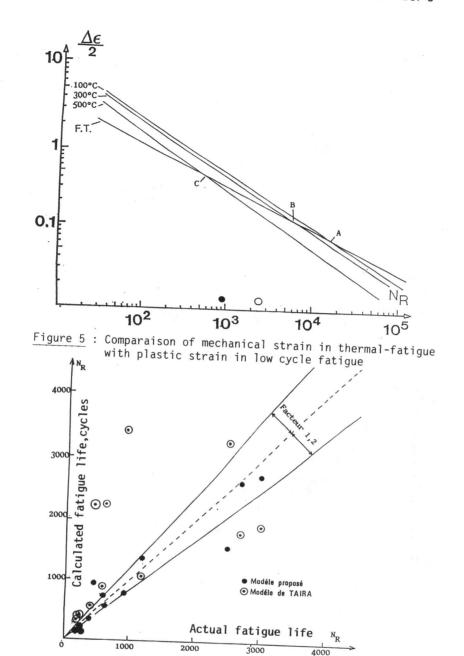


Figure 6 : Comparison of actual thermal-mechanical fatigue life with cyclic life calculated from isothermal fatigue curves